▸ LUCIANO SALVETTI, *Equivalence of generics: an introduction and open problems.*
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One of the most important open problems in the theory of countable Borel equivalence relations (CBERs) reads ([4]): is every hyper-hyperfinite CBER (i.e., countable increasing union of hyperfinite equivalence relations) hyperfinite? One interesting example of an hyper-hyperfinite CBER which is not known to be hyperfinite is the equivalence of Cohen generics studied by Smythe in [8]. More generally, given a countable transitive model M of (a large fragment of) ZFC and a forcing notion $\mathbb{P} \in M$ we say that two generic filters are equivalent if they produce the same generic extension of M. Combinatorial properties of the poset $\mathbb{P}$ yield dynamical properties of the CBER and viceversa. In this talk we will go over some results about this class of CBERs for well-known forcing notions (Cohen, random, Prikry, etc) and open problems in the literature ([2], [8]). Time permitting, we will also describe a comeagre set of Cohen reals where Cohen equivalence becomes hyperfinite, using an argument that involves Borel combinatorics and avoids the generic hyperfiniteness theorem. This last part will be a section of the author's PhD thesis.

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