

- NATHAN CARLSON, *Cardinal inequalities using  $o$ -free sequences.*

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We introduce the notion of an  $o$ -free sequence, related to a free sequence, and show several cardinal inequalities. Modifying recent work of Angela Bella, we show that if  $X$  is a compact Hausdorff space then  $w(X) \leq hL(X)^{ot(X)}$ . (The  $o$ -tightness  $ot(X)$ , introduced by Tkachenko, has the properties  $ot(X) \leq t(X)$  and  $ot(X) \leq c(X)$ ). A cardinality bound for compact Hausdorff spaces follows which is shown to be a strict improvement of Arhangel'skii's well-known bound  $2^{\psi(X)}$ . We also give a characterization of the  $o$ -tightness in compact Hausdorff spaces using weak  $o$ -free sequences. This work has appeared in [1]

[1] N. CARLSON, *On  $o$ -free sequences and compacta*, *Topology and its Applications*, vol. 377 (2026), 109631.