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Laver forcing, denoted $\mathbb{L}$, originates in Richard Laver's seminal work on the consistency of the Borel conjecture and iterated forcing techniques [5]. Since then, $\mathbb{L}$ and its restricted variant $\mathbb{L}_{\mathcal{U}}$ for an ultrafilter $\mathcal{U}$ on ω have played central roles in combinatorial set theory and the set theory of the real line.

One of the key features of Laver forcing is the *Laver property*, which provides strong control over the reals in the generic extension and is preserved under countable support iterations of proper forcing notions. A natural question, therefore, is to determine when the restricted forcing $\mathbb{L}_{\mathcal{U}}$ retains the Laver property of $\mathbb{L}$. In this talk, we introduce *Laver ultrafilters*: ultrafilters $\mathcal{U}$ for which $\mathbb{L}_{\mathcal{U}}$ has the Laver property. We give simple combinatorial characterizations of this class and establish connections with several well-studied families of ultrafilters, including P-points, rapid ultrafilters, and ultrafilters arising from Baumgartner's $\mathcal{I}$-ultrafilter framework [1]. As a consequence, we improve a result of Błaszczyk and Shelah on when $\mathbb{L}_{\mathcal{U}}$ adds Cohen reals [2].

Finally, we will discuss the (generic) existence of Laver ultrafilters and establish bounds on their *generic existence number*, a notion defined by Brendle and Flašková [3], in terms of well-studied cardinal invariants of the continuum. As an application, we construct a model of set theory in which Laver ultrafilters exist generically, while no P-points exist at all.

This is work in progress with Silvan Horvath [4].

[1] J. E. Baumgartner, *Ultrafilters on ω*, ***The Journal of Symbolic Logic***, vol. 60 (1995), no. 2, pp. 624–639.

[2] A. Błaszczyk and S. Shelah, *Regular subalgebras of complete Boolean algebras*, ***The Journal of Symbolic Logic***, vol. 66 (2001), no. 2, pp. 792–800.

[3] J. Brendle and J. Flašková, *Generic existence of ultrafilters on the natural numbers*, ***Fundamenta Mathematicae***, vol. 236 (2017), no. 3, pp. 201–245.

[4] S. Horvath and T. Özalp, *Laver ultrafilters*, in preparation.

[5] R. Laver, *On the consistency of Borel's conjecture*, ***Acta Mathematica***, vol. 137 (1976), no. 3-4, pp. 151–169.