

- ▶ JOEL KUPERMAN, *A characterization of the partial orders associated to right-normal bands.*

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The variety of bands (idempotent semigroups) and its subvarieties were studied by Gerhard in [1]. The equation  $x \cdot y = x$  determines a preorder on algebras in this variety, and it is a partial order if and only if the algebras satisfy the additional condition  $x \cdot y \cdot x = y \cdot x$ . The subvariety of algebras satisfying this equation is the variety of right-regular bands (RRB). Semilattices, for example, form a subvariety of the right-regular bands. The partial order underlying the latter is well understood, but the same is not true for other subvarieties ([2]).

We consider the subvariety determined by bands satisfying the identity  $x \cdot y \cdot z = y \cdot x \cdot z$ . This is the variety of right-normal bands. We call the posets underlying right-normal bands *normal posets*. We present a result that characterizes normal posets in a purely order-theoretical manner and discuss some of the difficulties in obtaining a similar result for right-regular bands in general.

[1] JAMES ARTHUR GERHARD, *The lattice of equational classes of idempotent semigroups*, *Journal of algebra*, vol. 15 (1970), no. 2, pp. 195–224.

[2] JOEL KUPERMAN, ALEJANDRO PETROVICH, PEDRO SANCHEZ TERRAF, *Definability of band structures on posets*, *Semigroup forum*, vol. 109 (2024), no. 3, pp. 537–557.